

# Approximate Computing

## 1. Introduction

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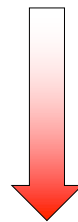
## Chapter Overview

- 1.1 What is Approximate Computing?
- 1.2 For whom is this course?
- 1.3 Course content & organization

## Motivation

- Try to quickly answer these questions:

1. Is 47.2 divided by 1.3 greater than 1?
2. Is 47.2 divided by 1.3 greater than 35?
3. What is 47.2 divided by 1.3?



required accuracy (effort)

- Computational accuracy should be task-dependent ...  
... yet, computers always (mostly) use the same accuracy

## Approximate Computing (AxC)

- The central idea of AxC is to trade-off computational accuracy for a reduction in effort, i.e.,
  - energy and/or
  - execution time and/or
  - hardware area.
- These are key concerns for today's computing devices



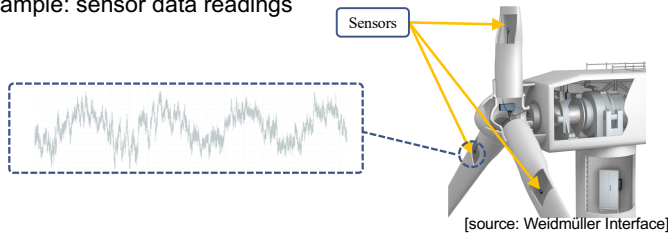
embedded / mobile systems



server farms

## Suitable Application Domains

- Redundant, noisy, imprecise or incomplete input data
  - example: sensor data readings

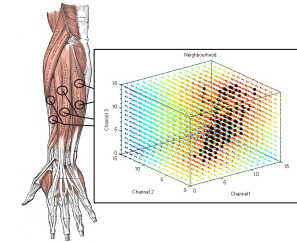


- Output perceived by humans with limited perception
  - example: JPEG lossy image compression



## Suitable Application Domains

- Time/energy constraints prohibit the computation of an exact or optimal result
  - examples: big data, machine learning

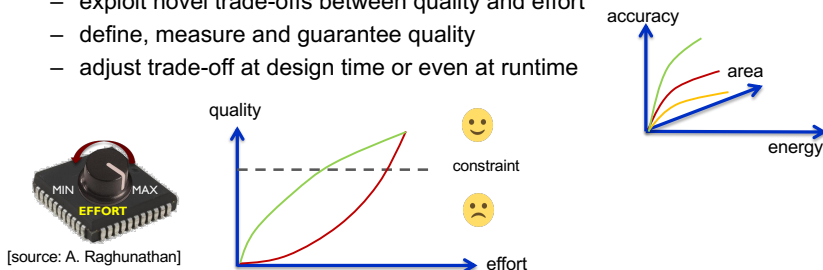


- No unique or golden answer exists
  - examples: search machines, recommender systems



## Quality-Effort Trade-Off

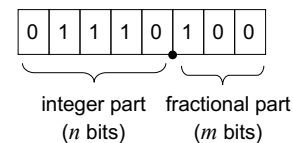
- 'Quality' as a new characteristic of an implementation
  - quality metric is **application-dependent**
    - examples: PSNR for image compression, classification accuracy for neural network, worst-case error for an arithmetic computation, user rating for a search engine ...
  - quality can be a **constraint** or an **optimization objective**
- New challenges for design and optimization
  - exploit novel trade-offs between quality and effort
  - define, measure and guarantee quality
  - adjust trade-off at design time or even at runtime



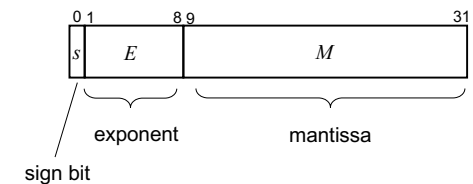
## Is AxC Really New? – Related Forms of AxC

- Finite machine precision
  - floating point data types always have limited precision
  - a floating point variable is an **approximation of a real number**
  - extensive work exists on studying quantization and rounding effects, error analysis, error propagation in longer computations, ...

Example: unsigned fixed-point number with precision (accuracy) of  $2^{-m}$



Example: floating-point number in single precision IEEE 754 standard format, precision is not constant over value range



## Is AxC Something New? – Related Forms of AxC

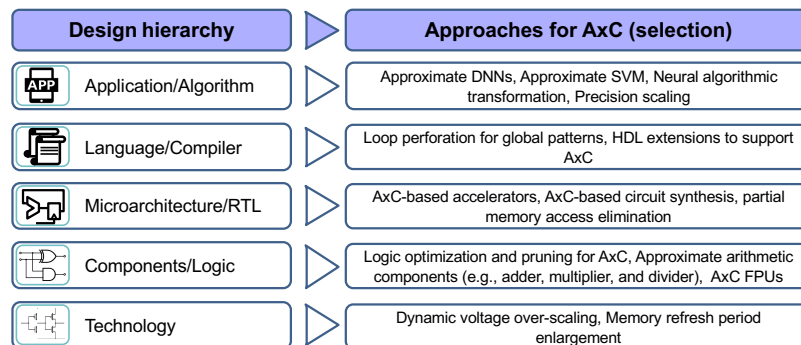
- Heuristics and approximation algorithms
  - a heuristic is an efficient algorithm for a problem **without a guarantee that the solution is accurate / exact / optimal**
  - an approximation algorithm is an efficient algorithm with a **proven distance between returned and optimal solution** (approximation factor)
- Anytime (iterative) algorithms
  - an anytime algorithm can **return a valid solution to a problem even if it is interrupted** before it ends
  - typically realized by iterative improvements of an initial valid solution
  - if running longer, the quality of the output increases
- Heuristics, approximation algorithms, and anytime algorithms **compute approximated solutions**

## Is AxC Something New? – Related Forms of AxC

- Unconventional computing paradigms that approximate solutions
    - **Stochastic Computing**
      - represent **numbers by streams of random bits**: with  $n$  as number of bits in the stream, and  $m$  as the number of '1's, the value is  $m/n$
- |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 |
|---|---|---|---|---|---|---|---|
- $3/8 = 0.375$
- requires little hardware for many operations and is tolerant against bit flips, but also slow and requires bit streams to be uncorrelated
  - **(Electronic) Analog Computing**
    - computers built from **electronic components**, such as diodes, resistors, operational amplifiers, etc.
    - can excel in speed and energy-efficiency, but suffer from low reliability, limited precision, errors, and cumbersome programming
  - **Probabilistic Computing**
    - analog computing where **signals express probabilities**
    - basically, same pros and cons as analog computing

## The (Re-)Emergence of AxC

- Current focus: Aggressively apply approximations **on and across all levels of the computer design hierarchy, including hardware**



## The (Re-)Emergence of AxC

- DARPA/ISAT Workshop 2012 on “Advancing computer systems without technology progress”
  - identified AxC as one approach for future performance gains

[C. Kozyrakis: “Advancing computer systems without technology progress”, IEEE International Symposium on Performance Analysis of Systems and Software, 2013]
- AxC workshop series
  - Workshop on Probabilistic and Approximate Computing (APPROX)
  - Workshop on Approximate Computing (WAPCO)
  - Workshop on Approximate Computing Across the Stack (WACAS)
  - Workshop on Approximate Computing (AC)
    - AC 2015 in Paderborn
- AxC sessions in several other conferences



## The (Re-)Emergence of AxC

- Increasing number of publications, also in popular magazines



Sampson et al.: "EnerJ, the Language of Good-Enough Computing", *IEEE Spectrum*, Oct. 2013



R. Nair: "Big Data Needs Approximate Computing". *Comm. ACM*, Jan 2015



L. Kugler: "Is 'good enough' computing good enough?" *Comm. ACM*, May 2015



C. Plessl, M. Platzner, P. Schreier: "Aktuelles Schlagwort: Approximate Computing", *Informatik Spektrum*, 2015



Special Issue on Approximate Computing in *IEEE Design & Test*, 2016

## Dependability vs. Approximation

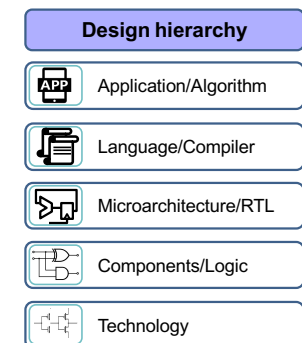
- Semiconductor technology progresses into low nm domain
  - **fault-free operation difficult to achieve** due to increasing densities and shrinking supply voltages
  - **dependability** of chips becomes a huge concern
    - guardbanding leads to diminishing returns
    - redundancy techniques show excessive overheads in hardware and/or software
  - currently unclear how long technology scaling will continue and when (and which) post-CMOS technologies will be ready
- AxC does not combat 'faults', but intentionally insert them
  - yet, same techniques could be useful for both approaches

## 1.2 For Whom is this Course

- Goals
  - **research-oriented advanced Master-level course**
  - introduce to the emerging field of Approximate Computing
  - provide an overview over approximation approaches at different levels
  - serve as a starting point for research activities
- Addressed study programs
  - **Computer Science (CS)** master students
    - elective module in focus area "Computer Systems"
  - **Computer Engineering (CE)** master students
    - elective module in focus areas "Computer Systems" and "Embedded Systems"
- Prerequisites
  - no formal prerequisites with respect to other Master-level courses
  - **HOWEVER: solid background in micro/nanoelectronics, digital design, computer architecture, and algorithms/applications is extremely helpful**

## 1.3 Course Content & Organization

- Lecture – Topics (tentatively)
  1. Introduction
  2. Application / algorithm level
  3. Language / compiler level
  4. Microarchitecture / register-transfer level
  5. Components / logic level
  6. Technology level



## Course Content & Organization

- Lecturers

Hassan Ghasemzadeh Mohammadi, O3.134, ☎ 60 4344, [hgm@mail.upb.de](mailto:hgm@mail.upb.de)



Marco Platzner, O3.207, ☎ 60 5250, [platzner@upb.de](mailto:platzner@upb.de)



- Lecture sessions

- Thursday 11:15 - 13:45

- Course uses the “inverted classroom model”

- elements of lecture and post-processing are swapped (inverted)
- learning activities that students can do well on their own are shifted to a preparation phase
- the common attendance time is used for an active discussion

## “Inverted Classroom” Model

- Advantage

- instead of frontal teaching, a time window is created for joint discussion and deepening of understanding
- the lecture material can be studied at any time, as often as desired, and from anywhere

- Implementation

- The lecturers make material available in PANDA (slides, screencast+audio)
- You prepare independently for the classroom sessions
- We use the common attendance times for
  - clarification of specific questions, discussions
  - examples, possibly small exercises, quizzes
  - reflection of the learning process

## Course Content & Organization

- Lab sessions

- two modules (successful participation of a module earns a bonus)
  - AxC for machine learning (ML)
    - AxC at the level of application/algorithm
    - get familiar with widely used ML libraries such as Scikit-learn and Tensor-flow
    - apply approximation on different groups of ML algorithms, e.g., clustering and classification
    - evaluate performance and quality of ML models using error analysis
  - AxC for digital signal processing (DSP) circuits
    - AxC at the levels of microarchitecture/RTL and components/logic
    - get familiar with a circuit AxC synthesis process
    - work with approximate component libraries
    - study quality evaluation of approximate DSP circuits
    - learn to work with commercial synthesis tools, e.g., Synopsys Design Compiler
- start of lab sessions will be announced

## Course Content & Organization

- Course materials

- all information is made available on PANDA:  
<https://panda.uni-paderborn.de/course/view.php?id=27940>

- Grading

- successful participation in the lab improves grade by 1 or 2 grade steps (if exam is passed)
- oral exam (~45') covering lecture + lab

## Positional and Survey Papers (Selection)

- J. Han and M. Orhansky. [Approximate Computing: An Emerging Paradigm for Energy-Efficient Design](#). IEEE European Test Symposium, 2013.
- A. Sampson, L. Ceze and D. Grossman. [Enerj, the Language of Good-Enough Computing](#). IEEE Spectrum, Oct 2013.
- R. Nair. [Big Data Needs Approximate Computing](#). Communications of the ACM, Dec 2014.
- L. Kugler. [Is “Good Enough” Computing Good Enough?](#) Communications of the ACM, Apr 2015.
- S. Mittal. [A Survey of Techniques for Approximate Computing](#). ACM Computing Surveys, Nr. 62, 2016.
- S. Davidson. [Good Enough Computing](#). IEEE Design & Test, 33(1), 2016.
- Q. Xu, T. Mytkowicz, and N.S. Kim. [Approximate Computing: A Survey](#). IEEE Design & Test, 33(1), 2016.
- G. Rodrigues, F.L. Kastensmidt, and A. Bosio. [Survey on Approximate Computing and Its Intrinsic Fault Tolerance](#). Electronics, 9(4):557, 2020.